

**INTERNATIONAL INDIAN SCHOOL - DAMMAM**

**SECOND TERM EXAMINATION- NOV .2014**

**CLASS : XII**

**SET – A**

**Max Marks : 100**

**Time: 3 hours**

**SUBJECT: MATHEMATICS**

**General Instructions:**

1. All questions are compulsory.
2. The question paper consists of 26 questions divided into three sections A, B, C, Section A contains 6 questions of 1 mark each, Section B is of 13 questions of 4 marks each and section C is of 7 questions of 6 marks each.
3. All questions in section A are to be answered in one word, one sentence or as per the requirement of the question.
4. There is no overall choice. However, internal choice has been provided in 4 questions of four marks each and 2 questions of six marks each. You have to attempt only one of the alternatives in all such questions.
5. Use of calculator is not permitted. You may ask for logarithmic tables, if required.

**Section. A**

1) What is the angle between vectors  $\vec{a}$  and  $\vec{b}$  with magnitude  $\sqrt{3}$  and 2 respectively

Given that  $\vec{a} \cdot \vec{b} = 3$

2) Find the general solution of the differential equation  $\frac{dy}{dx} = \frac{1+y^2}{1+x^2}$ .

3) If  $f(1) = 4$ ,  $f'(1) = 2$ , find the value of derivative of  $\log f(e^x)$  w.r.t.  $x$  at the point  $x = 0$ .

4) Evaluate  $\int_{-1}^1 \sin^5 x \cdot \cos^4 x \, dx$ .

5) Find the value of  $\lambda$  so that the vectors  $\vec{a} = 2\hat{i} + \lambda\hat{j} + \hat{k}$  and  $\vec{b} = \hat{i} - 2\hat{j} + 3\hat{k}$  are perpendicular to each other.

6) Find the slope of the tangent to the curve  $x = t^2 + 3t - 8$ ,  $y = 2t^2 - 2t - 5$  at  $t = 2$ .

**Section. B**

7) Form the differential equation of the family of ellipse having foci on Y axis and centre at the origin.

8) Let vector  $\vec{a} = \hat{i} + 4\hat{j} + 2\hat{k}$ ,  $\vec{b} = 3\hat{i} - 2\hat{j} + 7\hat{k}$  and  $\vec{c} = 2\hat{i} - \hat{j} + 4\hat{k}$ . Find a vector  $\vec{d}$  which is perpendicular to both  $\vec{a}$  and  $\vec{b}$  and  $\vec{c} \cdot \vec{d} = 15$ .

OR

Using vectors find the area of the triangle with vertices  $A(1,1,2)$ ,  $B(2,3,5)$  and  $C(1,5,5)$ .

9) Using properties of definite integrals evaluate  $\int_0^{\frac{\pi}{4}} \log(1 + \tan x) dx$ .

10) Find the relationship between 'a' and 'b' so that the function  $f$  defined by

$$f(x) = \begin{cases} ax + 1, & \text{if } x \leq 3 \\ bx + 3, & \text{if } x > 3 \end{cases} \text{ is continuous at } x = 3.$$

11) Evaluate  $\int \frac{3x-1}{(x+2)^2} dx$ .

OR

Evaluate  $\int e^{2x} \sin x dx$ .

12) Show that the four points A, B, C, and D with position vectors  $4\hat{i} + 5\hat{j} + \hat{k}$ ,  $-\hat{j} - \hat{k}$ ,  $3\hat{i} + 9\hat{j} + 4\hat{k}$  and  $4(-\hat{i} + \hat{j} + \hat{k})$ , respectively are coplanar.

13) Find the intervals in which the function  $f$  is given by  $f(x) = \sin x + \cos x$ ,  $0 \leq x \leq 2\pi$  is strictly increasing or strictly decreasing.

14) Find  $\frac{dy}{dx}$  if  $x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$ .

OR

If  $y = \log \left[ x + \sqrt{x^2 + 1} \right]$  prove that  $(x^2 + 1) \frac{d^2y}{dx^2} + x \frac{dy}{dx} = 0$ .

15) Find the particular solution of the differential equation  $\frac{dy}{dx} + 2y \tan x = \sin x$ .  $y = 0$ , when  $x = \frac{\pi}{3}$ .

16) Find the area of the region bounded by the two parabolas  $y = x^2$  and  $y^2 = x$ .

OR

Find the area of the region bounded by the parabola  $y = x^2$  and  $y = |x|$ .

17) Prove that the curves  $x = y^2$  and  $xy = k$  cut at right angles if  $8k^2 = 1$ .

18) Using integration find the area of the triangular region whose vertices are  $(-1, 0)$ ,  $(1, 3)$  and  $(3, 2)$ .

19) Solve the differential equation  $2x^2 \frac{dy}{dx} - 2xy + y^2 = 0$

### Section -C

20) Evaluate  $\int_0^{\frac{\pi}{4}} \frac{\sin x + \cos x}{9 + 16 \sin 2x} dx$ .

OR

Evaluate  $\int_0^{\frac{\pi}{2}} \frac{\cos^2 x}{\cos^2 x + 4 \sin^2 x} dx$ .

21) Solve the differential equation  $3e^x \tan y dx + (2 - e^x) \sec^2 y dy = 0$ , given that

$$x = 0, y = \frac{\pi}{4}$$

22) Using integration, find the area of the region  $\{(x, y) \mid |x-1| \leq y \leq \sqrt{5-x^2}\}$

OR

Find the area of the region enclosed between the two circles

$$x^2 + y^2 = 4 \text{ and } (x-2)^2 + y^2 = 4$$

23) Differentiate  $y = (\sin x)^x + \sin^{-1} \sqrt{x}$  w.r.t.  $x$ .

24) Evaluate  $\int_1^4 (x^2 - x) dx$  as limit of sums.

25) Three vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  satisfy the condition  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$ . Evaluate the quantity

$$\mu = \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}, \text{ if } |\vec{a}| = 1, |\vec{b}| = 4 \text{ and } |\vec{c}| = 2.$$

(b) Find a vector of magnitude 5 units, and parallel to the resultant of the vectors

$$\vec{a} = 2\hat{i} + 3\hat{j} - \hat{k} \text{ and } \vec{b} = \hat{i} - 2\hat{j} + \hat{k}.$$

26) A window is in the form of a rectangle surmounted by an equilateral triangle. The total perimeter of the window is 12 m. Find the dimensions of the rectangle that will produce the largest area of the window ?

How large windows help us in saving electricity and conserving environment ?

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